Week of April 16, 2018

Find all real-valued continuously differentiable

functions f on the real line such that for all x

$$(f(x))^{2} = \int_{0}^{x} \left[(f(t))^{2} + (f'(t))^{2} \right] dt + 1990$$