Week of September 10, 2018

Find the maximum value of

$$\int_0^y \sqrt{x^4 + (y - y^2)^2} \, dx \quad \text{for } 0 \le y \le 1.$$

Putnam 1991-A5